

ADVANCED ENGINEERING NUMERICAL METHODS and COMPUTER PROGRAMMING

THEORY AND PRACTICAL



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MACMILLAN

Contents

Preface	vii
Syllabus	ix
1 Approximation in Numerical Computation, Errors	1
1.1 Introduction	1
1.2 Mathematical preliminaries	1
1.3 Approximation in Numerical Computation	2
1.4 Floating-Point Form of Numbers	3
1.5 Approximate Numbers, Rounding-off Numbers and Significant Figures	4
1.5.1 Approximate numbers	4
1.5.2 Round off of a number	4
1.5.3 Significant figures	4
1.6 Several Type of Errors	6
1.6.1 Iteration error	6
1.6.2 Approximation error	6
1.6.3 Inherent errors and rounding-off errors	6
1.6.4 Truncation error	7
1.7 Errors and their Computation	7
1.8 Application of Error Formula	10
1.9 Error in Evaluation of a Function of Several Variables	11
1.10 Error in a Series Approximation	12
1.11 Uncertainty in Data or Noise	13
1.12 Significant Error	13
1.13 Multiple Choice Questions (MCQ)	19
2 Calculus of Finite Difference	23
2.1 Forward Difference	23
2.2 Backward Difference	25
2.3 Relation between Forward and Backward Differences	26
2.4 Other Symbolic Operator and their Relations	27
2.5 Properties of Forward Difference Operator Δ	27
2.6 Properties of Shift Operator E	27
2.7 Newton-Gregory Formula	28
2.8 Evaluation of Missing Term in the Given Datas	28
2.9 Factorial Notation	29

2.10	Propagation of Errors in a Difference Table	29
2.11	Divided Differences	30
2.12	Multiple Choice Questions (MCQ)	41
3	Interpolation	45
3.1	Interpolation	45
3.1.1	Introduction	45
3.1.2	Difference between interpolation and extrapolation	46
3.1.3	Weirstrass approximation theorem	46
3.2	Theorem of Polynomial Interpolation	47
3.3	Lagrange's Interpolation	47
3.3.1	Lagrange's interpolation formula for equally spaced points	48
3.3.2	Uniqueness of Lagrange's interpolating polynomial	48
3.3.3	The error in the Lagrange's interpolating polynomial/error of interpolating polynomial	48
3.4	Newton's Interpolation	51
3.4.1	Newton's forward difference interpolation formula	51
3.4.2	Newton's backward interpolation	54
3.5	Divided Differences Formula	56
3.5.1	Properties of divided difference	57
3.5.2	Divided difference for equispaced arguments	58
3.5.3	Confluent divided differences	58
3.5.4	Deduction of some important formula	59
3.5.5	Newton's fundamental interpolation formula by divided difference formula	60
3.5.6	Newton's divided difference interpolation formula	61
3.5.7	Taylor's Theorem	62
3.5.8	Newton divided to Newton's forward formula	63
3.5.9	Newton divided to Newton's backward formula	63
3.6	Gauss's Central Difference Interpolation	64
3.6.1	Gauss forward difference interpolation for odd $(2n+1)$ equispaced arguments	64
3.6.2	Gauss forward difference interpolation for even $(2n)$ equispaced arguments	65
3.6.3	Gauss backward difference interpolation for odd $(2n+1)$ equispaced arguments	66
3.6.4	Gauss backward difference interpolation for even $(2n)$ equispaced arguments	66
3.6.5	Stirling's interpolation formula	67
3.7	Interpolation by Iteration (Aitken's Interpolation)	68
3.8	Multiple Choice Questions (MCQ)	76
4	Inverse Interpolation	81
4.1	Inverse Interpolation	81
4.1.1	Inverse interpolation based on Lagrange's interpolation formula for unequally spaced points	83
4.1.2	Inverse interpolation based on Newton's forward difference interpolation formula	84

4.1.3	Inverse interpolation based on Newton's backward difference interpolation formula	84
4.1.4	Inverse interpolation for odd $(2n + 1)$ equispaced arguments based on Gauss's forward difference interpolation formula	85
4.1.5	Inverse interpolation for even $2n$ equispaced arguments based on Gauss's forward difference interpolation formula	86
4.2	Inverse Interpolation Formula using Divided Difference Interpolation Formula	86
4.3	Application of the Inverse Interpolation Formula to Find a Root of a Equation	87
4.4	Multiple Choice Questions (MCQ)	90
5	Numerical Differentiation	93
5.1	Introduction	93
5.2	Error in Numerical Differentiation Formula	93
5.2.1	Differentiation based on Lagrange's interpolation polynomial	94
5.2.2	Differentiation based on Newton's forward interpolation polynomial	96
5.2.3	Differentiation based on Newton's backward interpolation polynomial	98
5.3	Differentiation Formula Based on Newton's Divided Difference Polynomial	99
5.4	Differentiation Formula Based on Taylor's Theorem	101
5.5	Multiple Choice Questions (MCQ)	105
6	Numerical Integration	109
6.1	Introduction	109
6.1.1	Degree of precision	110
6.2	General or Gauss-Legendre Quadrature Formula (Closed Type)	110
6.2.1	Dependent on Newton's forward difference interpolating polynomial	110
6.2.2	Derivation of trapezoidal rule	111
6.2.3	Composite trapezoidal rule	112
6.2.4	Simpson's 1/3 rule	113
6.2.5	Composite Simpson's 1/3 rule	114
6.2.6	Newton-Cotes' closed type numerical integration formula	115
6.2.7	Trapezoidal rule from Newton-Cotes, formula	117
6.2.8	Simpson's 1/3 rule from Newton-Cotes, formula	117
6.2.9	Simpson's 3/8 rule from Newton-Cotes, formula	118
6.2.10	Weddle's rule from Newton-Cotes, formula	118
6.2.11	Geometrical interpretation of trapezoidal rule	119
6.2.12	Geometrical interpretation of Simpson's 1/3 rule	119
6.2.13	Legendre-gauss quadrature formula	120
6.2.14	Euler-Maclaurin sum formula	120

